

| Samples | x | y | $x - \bar{x}$ | $y - \bar{y}$ | $(x - \bar{x})^2$ | $(y - \bar{y})^2$ | $(x - \bar{x})(y - \bar{y})$ |
|--------------------|------------|--------------|---------------|---------------|-------------------|---------------------|------------------------------|
| 1 | 15 | 2289 | -2 | -715.1 | 4 | 511,368.01 | 1,430.20 |
| 2 | 17 | 3393 | 0 | 388.9 | 0 | 151,243.21 | - |
| 3 | 18 | 3271 | 1 | 266.9 | 1 | 71,235.61 | 266.90 |
| 4 | 15 | 2648 | -2 | -356.1 | 4 | 126,807.21 | 712.20 |
| 5 | 16 | 2897 | -1 | -107.1 | 1 | 11,470.41 | 107.10 |
| 6 | 19 | 3327 | 2 | 322.9 | 4 | 104,264.41 | 645.80 |
| 7 | 17 | 2970 | 0 | -34.1 | 0 | 1,162.81 | - |
| 8 | 16 | 2535 | -1 | -469.1 | 1 | 220,054.81 | 469.10 |
| 9 | 18 | 3138 | 1 | 133.9 | 1 | 17,929.21 | 133.90 |
| 10 | 19 | 3573 | 2 | 568.9 | 4 | 323,647.21 | 1,137.80 |
| Total | 170 | 30041 | | | 20 | 1,539,182.90 | 4,903.00 |
| Square root | | | | | 4.47 | 1,240.64 | |
| | \bar{x} | 17 | | | | | |
| | \bar{y} | 3004.1 | | | | | |
| | n | 10 | | | | | |

Part i)

$$r = \frac{\sum(x - \bar{x})(y - \bar{y})}{\sqrt{\sum(x - \bar{x})^2} \sqrt{\sum(y - \bar{y})^2}} = \frac{4903}{4.47 \times 1240.64} = 0.88 = 88\%$$

It means strong positive linear relationship between maternal age and birth weight of baby.

Part ii)

$$r^2 = 0.88^2 = 0.77 = 77\%$$

So, 77% of the variability in birth weight of baby can be explained by the variability of maternal age.

Part iii)

$$S_y = \sqrt{\frac{\sum(y - \bar{y})^2}{(n - 1)}} = \sqrt{\frac{1,539,182.90}{(10 - 1)}} = \sqrt{171,020.32} = 413.55$$

$$S_x = \sqrt{\frac{\sum(x - \bar{x})^2}{(n - 1)}} = \sqrt{\frac{20}{(10 - 1)}} = \sqrt{2.2} = 1.49$$

$$\beta_1 = r \frac{S_y}{S_x} = 0.88 \frac{413.55}{1.49} = 244.24$$

$$\beta_0 = \bar{y} - \beta_1 \bar{x} = 3,004.1 - 244.24 \times 17 = 3,004.1 - 4,152.08 = -1,147.98$$

$$y = \beta_1 x + \beta_0 = 244.24 x - 1,147.98$$

Part iv)

$x = 20$

$$y = 244.24 X (20) - 1,147.98 = 4,884.8 - 1,147.98 = 3,736.82 \text{ grams}$$

$x = 40$

$$y = 244.24 X (40) - 1,147.98 = 9,769.6 - 1,147.98 = 8,621.62 \text{ grams}$$

v). Plot the data and draw a trend line

